EXAMPLE M: SIMPLIFY EXPRESSIONS

Name: __________________________

Directions: Simplify each.

1. \[
\frac{2w^2 - 50}{x^2 - 4w - 5}
\]

2. \[
\frac{-3w^2 - 9w + 54}{w^2 - 9w + 18}
\]

3. \[
\frac{16v^4w^2}{12w^2 + 20u^4w}
\]
**MORE TRANSPARENT**

Revised EXAMPLE M: SIMPLIFY EXPRESSIONS

Used by permission of Dr. Trina Palmer, Appalachian State University

MAT 1531 Simplification

Due: September 20

**Purpose:**
The purpose of this assignment is to (1) improve your mathematical writing and (2) demonstrate your algebraic manipulation skills. This assignment will help prepare you for simplifying expressions from calculus and help you communicate where your understanding and misunderstanding are. Knowing how to simplify expressions is like using correct grammar -- it makes the written mathematics easier to read and understand. Real-life modeling problems are everywhere such as modeling the spread of COVID-19 or predicting future global temperatures. Simplifying the mathematical models as they are developed reduces possible errors.

**Student Learning Outcomes addressed in this assignment:**
1. Simplify Algebraic Expressions
2. Communicate algebraic reasoning

**Assignment:**
Simplify one of the following problems, and include justifications for each manipulation.

1. \[
\frac{2w^2 - 50}{x^2 - 4w - 5}
\]
2. \[
\frac{-3w^2 - 9w + 54}{w^2 - 9w + 18}
\]
3. \[
\frac{16v^4w^2}{12w^2 + 20u^4w}
\]

**Sample Problem**

<table>
<thead>
<tr>
<th>Simplify: ( \frac{w^2 - 7u + 6}{5 - 5u^2} )</th>
<th>(- (u + 7) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Answer: ( \frac{5(1 + u)}{} )</td>
<td>Restatement</td>
</tr>
<tr>
<td>( \frac{u^2 - 7u + 6}{5 - 5u^2} )</td>
<td>Factor the numerator and denominator</td>
</tr>
<tr>
<td>( \frac{(u + 7)(u - 1)}{5(1 - u^2)} )</td>
<td>Factor the denominator (difference of two squares)</td>
</tr>
<tr>
<td>( \frac{- (u + 7)(1 - u)}{5(1 - u)(1 + u)} )</td>
<td>Factor out a negative one in the numerator</td>
</tr>
<tr>
<td>( \frac{- (u + 7) \frac{(1 - u)}{5(1 + u)}}{5(1 + u)} )</td>
<td>Rearrange factors (commutative property of multiplication)</td>
</tr>
<tr>
<td>( \frac{- (u + 7)}{5(1 + u)} )</td>
<td>Multiplicative identity</td>
</tr>
</tbody>
</table>

Trina Palmer
<table>
<thead>
<tr>
<th>Criteria:</th>
<th>Proficient</th>
<th>Emerging</th>
<th>Needs Improvement</th>
</tr>
</thead>
<tbody>
<tr>
<td>Algebraic accuracy</td>
<td>Includes most steps and steps are accurate</td>
<td>missing a few steps and/or some steps are inaccurate</td>
<td>many missing steps and/or many inaccurate steps</td>
</tr>
<tr>
<td></td>
<td>(5)</td>
<td>(3)</td>
<td>(1)</td>
</tr>
<tr>
<td>Mathematics language</td>
<td>reasoning is correct and mostly correct math language</td>
<td>reasoning is mostly correct and mostly correct mathematics language</td>
<td>Much of the reasoning and language is incorrect</td>
</tr>
<tr>
<td></td>
<td>(5)</td>
<td>(3)</td>
<td>(1)</td>
</tr>
</tbody>
</table>